

## Refinement of the Crystal and Molecular Structure of Cyclohexylammonium Chloride (Cyclohexylamine Hydrochloride)

By S. T. RAO\* AND M. SUNDARALINGAM†

*Department of Chemistry, Case Western Reserve University, Cleveland, Ohio 44106 U.S.A.*

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The present refinement of the crystal structure of cyclohexylammonium chloride represents an accurate determination of the simplest cyclohexane derivative known to date. Crystals of cyclohexylammonium chloride belong to the orthorhombic space group *Pca*2<sub>1</sub>, with four molecules in the unit cell of dimensions  $a = 9.313 \pm 0.001$ ,  $b = 11.442 \pm 0.002$  and  $c = 7.554 \pm 0.001$  Å,  $D_m = 1.14$  g.cm<sup>-3</sup>,  $D_x = 1.13$  g.cm<sup>-3</sup>. Intensities of 615 reflections were measured on a Picker four-circle diffractometer with Ni-filtered Cu radiation. All of the fourteen hydrogen atoms were unambiguously located on a difference electron density map. The structure was refined by full-matrix least-squares to an *R* value of 0.039 from 610 observed reflections, excluding five extinguished reflections. The cyclohexane ring is in the chair form with an equatorially substituted ammonium group. The average values of the bond distances, bond angles and the torsion angles in the ring are  $1.523 \pm 0.007$  Å,  $111.3 \pm 0.6^\circ$  and  $55.2 \pm 1.2^\circ$  respectively. The ammonium group is staggered to the ring; it is hydrogen bonded to three neighboring chloride ions and forms the stabilizing force in the crystal lattice. The average N-H $\cdots$ Cl<sup>+</sup> hydrogen-bond distance is 3.18 Å.

### Introduction

In this paper is reported the redetermination of the crystal structure of cyclohexylammonium chloride whose structure was originally derived by Shimada, Okaya & Nakamura (1955) with the use of projection data. The difficulty in obtaining adequate single crystals and the possibility of disorder in the crystal have remained obstacles to the solution of the crystal structure of cyclohexane itself by X-ray diffraction techniques. Current interest in the accurate geometry and conformation of cyclohexane and its derivatives prompt-

ted us to carry out this precise X-ray analysis of the simplest cyclohexane derivative known to date.

### Experimental

Crystals of cyclohexylammonium chloride, grown from aqueous ethanol solution, were in the form of plates. The lattice parameters were determined from six reflections with  $2\theta > 60^\circ$  carefully measured on a Picker four-circle diffractometer using nickel-filtered Cu radiation ( $\lambda = 1.5418$  Å). The crystal data are given in Table 1. The cell edges  $a$ ,  $b$  are shorter than those of the earlier investigation by about 0.5%, while that of  $c$  is about 2% greater. The crystal was mounted with the  $c$  axis parallel to the  $\varphi$  axis of the goniostat and 716 intensity data were scanned with Ni-filtered Cu radiation on a Picker four-circle diffractometer equipped

\* Present address: Department of Biochemistry, University of Wisconsin, Madison, Wisconsin 53706, U.S.A.

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Table 1. *Crystallographic data*

	This work Diffractometric	Shimada <i>et al.</i> (1955) Photographic
<i>a</i>	$9.313 \pm 0.001$ Å	$9.36 \pm 0.03$ Å
<i>b</i>	$11.442 \pm 0.002$	$11.47 \pm 0.03$
<i>c</i>	$7.554 \pm 0.001$	$7.41 \pm 0.03$
Crystal system	Orthorhombic	
Systematic absences	$0kl, l = 2n + 1$ $h0l, h = 2n + 1$	
Space group	<i>Pca</i> 2 <sub>1</sub> or <i>Pcam</i> ; <i>Pca</i> 2 <sub>1</sub> confirmed by intensity statistics and structure analysis	
<i>Z</i>	4	
<i>D<sub>x</sub></i>	1.13 g.cm <sup>-3</sup>	
<i>D<sub>m</sub></i>	1.14 g.cm <sup>-3</sup>	

with a scintillation counter and a pulse-height discriminator out to  $2\theta=134^\circ$ . Inspection of the systematically absent reflections ( $0kl$ ,  $l$  odd;  $h0l$ ,  $h$  odd) indicated that a reflection count is significant if  $I > 1.40(I)$ , where

$$\sigma(I) = [I_{\text{scan}} + I_{\text{bkg}}]^{1/2}.$$

On this criterion, 615 reflections were considered observed, and were used in the structure analysis. The total number of reflections accessible to Cu  $K\alpha$  radiation is about 930. The data were corrected for the Lorentz and polarization factors. The anisotropy of absorption was roughly accounted for by observing the intensity of a reflection at  $\chi=90^\circ$  as a function of  $\phi$ . The maximum variation in the intensity was 2%. Absorption corrections were not applied because the crystal used was small,  $0.1 \times 0.25 \text{ mm}^2$  in cross-section and 0.4 mm long. The distribution of the intensities (normalized structure amplitudes) showed that the space group is acentric. Therefore, the space group  $Pca2_1$  was assigned and the structure analysis and refinement were carried out on this basis (Shimada *et al.*, 1955).

### Structure determination and refinement

The structure was redetermined to confirm the results obtained by Shimada *et al.* (1955) who used two-dimensional data.

The  $x$  and  $y$  coordinates of the chloride were found from a gradient-sharpened three-dimensional Patterson diagram (Jacobson, Wunderlich & Lipscomb, 1961) and the  $z$  coordinate, which is arbitrary, was set equal to 0.0. A three-dimensional electron density distribution phased on this atom contained the spurious mirror symmetry. The nitrogen atom could be easily located and a second round of calculation using both the chloride and the nitrogen atoms revealed the entire structure, which was essentially the same as that obtained in the earlier work.

Four cycles of full-matrix least-squares refinement (Busing, Martin & Levy, 1962) using Hughes's (1941) weighting scheme lowered the  $R$  value from 0.350 to 0.104. The quantity minimized in the least-squares refinement was  $\sum w(|F_o| - k|F_c|)^2$ . At this point, a three-dimensional difference electron density map revealed the approximate positions of all the fourteen hydrogen atoms (Fig. 1). The hydrogen atoms were assigned a uniform thermal parameter of  $5 \text{ \AA}^2$  which was held fixed throughout the refinement. An additional three cycles of isotropic least-squares with the same weighting scheme reduced the  $R$  value to 0.064. Further cycles of

refinement were made in which the overall scale factor, positional parameters of the hydrogen atoms and the positional and anisotropic thermal parameters of the heavy atom were varied.

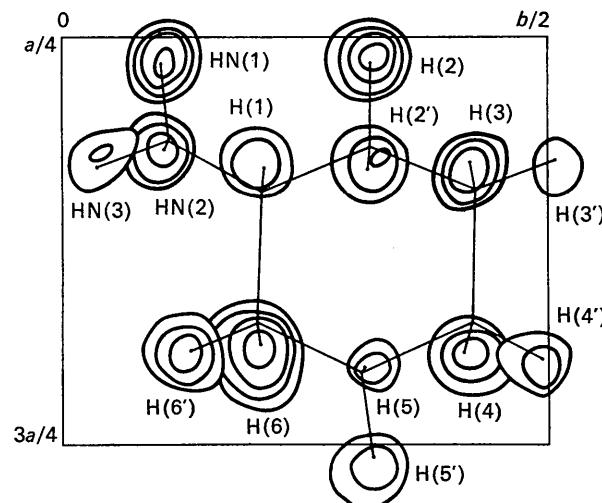


Fig. 1. The difference electron density map showing the hydrogen atoms. Contours are at intervals of  $0.1 \text{ e.}\text{\AA}^{-3}$  starting from  $0.2 \text{ e.}\text{\AA}^{-3}$ .

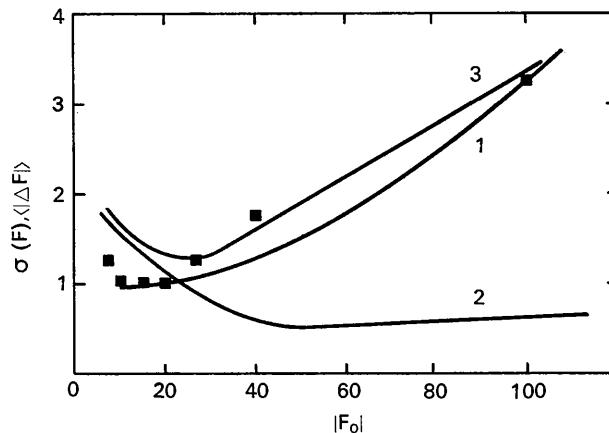


Fig. 2. A plot of the three different error schemes as a function of  $|F|$  used in the refinement. They are (1)  $\sigma_1(F) = [1.1 + |F| + 0.008|F|^2]^{1/2}$ , (2)  $\sigma_2(F) = \frac{F}{2} \cdot \frac{|I + B + 0.01(I + B)^2|^{1/2}}{|I - B|}$ , (3)  $\sigma_3(F) = \sigma_2(F) + 0.027|F|$ . The actual values of  $\langle \Delta|F_o - F_c| \rangle$  are shown by rectangles. Scheme 1 underestimates the errors in the weak reflections while scheme 2 underestimates the errors in the strong reflections. Scheme 3 reflects the proper errors.

Table 2. Some results of the refinement based on the three different weighting schemes

	$\Delta/\delta$	Average shift/standard deviation in positional parameters	$R$	$wR$	$\sqrt{\frac{w(\Delta F^2)}{m-n}}$	Average standard deviation in carbon atom positions	$C(4)-C(5)$
Scheme 1	0.38	0.042	0.054	1.28	0.006 Å	1.484 Å	
Scheme 2	0.19	0.041	0.036	2.16	0.005	1.486	
Scheme 3	0.16	0.039	0.050	1.02	0.006	1.493	

Table 3. Positional and thermal parameters of the atoms

	$x/a \times 10^4$	$y/b \times 10^4$	$z/c \times 10^4$	$\beta_{11} \times 10^4$	$\beta_{22} \times 10^4$	$\beta_{33} \times 10^4$	$\beta_{12} \times 10^4$	$\beta_{13} \times 10^4$	$\beta_{23} \times 10^4$
C(1)	4404 (5)	2064 (4)	39 (13)	107 (5)	67 (3)	143 (8)	-2 (3)	-2 (12)	1 (9)
C(2)	3834 (6)	3203 (5)	-710 (11)	107 (7)	65 (4)	247 (14)	17 (4)	-13 (8)	3 (6)
C(3)	4460 (7)	4244 (6)	275 (14)	137 (6)	75 (4)	271 (24)	7 (4)	23 (13)	-33 (9)
C(4)	6091 (7)	4210 (5)	276 (11)	139 (7)	69 (4)	222 (20)	-17 (4)	9 (11)	-21 (8)
C(5)	6662 (7)	3075 (6)	951 (12)	121 (8)	87 (5)	242 (14)	-7 (5)	-18 (9)	25 (8)
C(6)	6033 (5)	2029 (4)	-26 (15)	104 (5)	71 (4)	238 (11)	11 (3)	-1 (15)	8 (11)
N	3800 (5)	1058 (4)	-962 (8)	114 (5)	55 (3)	191 (9)	1 (3)	-8 (6)	15 (5)
Cl	455 (1)	1305 (1)	0	107 (1)	72 (1)	164 (2)	-9 (1)	-7 (3)	4 (2)
	$x \times 10^3$	$y \times 10^3$	$z \times 10^3$						
HN(1)*	262 (6)	108 (4)	-78 (9)						
HN(2)	404 (7)	113 (5)	-228 (9)						
HN(3)	415 (6)	32 (6)	-63 (8)						
H(1)	407 (7)	208 (6)	114 (9)						
H(2)	411 (7)	317 (6)	-196 (9)						
H(2')	274 (6)	316 (4)	-73 (9)						
H(3)	430 (7)	425 (6)	141 (10)						
H(3')	405 (6)	497 (5)	-58 (8)						
H(4)	634 (7)	433 (6)	-116 (9)						
H(4')	650 (6)	487 (5)	83 (10)						
H(5)	646 (7)	293 (6)	203 (11)						
H(5')	776 (7)	307 (5)	64 (8)						
H(6)	634 (7)	199 (6)	-133 (10)						
H(6')	635 (6)	133 (5)	36 (9)						

\* All hydrogen atoms are isotropic with  $B=5 \text{ \AA}^2$ .

The final stages of the anisotropic refinement were carried out with a Crickshank type of weighting scheme (scheme 1), where

$$\frac{1}{w} = \sigma_1(F) = [1.1 + |F| + 0.008|F|^2]^{1/2}.$$

After four cycles, convergence was reached, Table 2. However, it was found that the C(4)-C(5) bond distance was only 1.484 Å, significantly shorter than the remaining endocyclic bonds, which averaged 1.519 ± 0.003 Å. A plot of  $|\Delta F|$  vs.  $|F|$  indicated that the weighting scheme, although satisfactory for medium and strong reflections, underestimated the errors in the weakest group of reflections, Fig. 2. A plot of  $\sigma(F)$ , based on counting statistics and electronic instability of 1% vs.  $|F|$  also shown in Fig. 2. Since scheme 2 does not account for systematic errors due primarily to secondary extinction effects, the errors in the strong reflections are underestimated. Nevertheless, two cycles of refinement were carried out using weighting scheme 2. The results are listed in Table 2. Now scheme 2 was modified to yield scheme 3 which reflects the correct relative error in the data. This was done by adding a linear term in  $|F|$  so as to bring the  $\sigma(F)$  to the same level as  $\langle |\Delta F| \rangle$  for strong reflections.  $\sigma_3(F)$  is given by

$$\sigma_3(F) = \sigma_2(F) + 0.027|F|.$$

Results of the refinement based on scheme 3 are shown in Table 2. It is seen that the  $R$  index and the  $\Delta/\sigma$  value are the lowest for the latter refinement. The parameters obtained from weighting scheme 3 are listed in Table 3, together with the standard deviations estimated from

the diagonal terms of the inverse normal matrix. The analysis of the thermal ellipsoids in terms of the principal axes is given in Table 4. The observed and calculated structure factors are listed in Table 5. A perspective view of the electron density is shown in Fig. 3. An ORTEP plot (Johnson, 1965) of the molecule is shown in Fig. 4.

Table 4. Analysis of the thermal ellipsoids in terms of the principal axes

	$i$	$u_i$	$l_i$	$m_i$	$n_i$
C(1)	1	0.216 Å	-0.989	0.150	0.004
	2	0.210	-0.145	-0.954	-0.261
	3	0.203	-0.035	-0.259	0.965
C(2)	1	0.266	0.088	-0.019	-0.996
	2	0.224	0.804	0.592	0.060
	3	0.200	0.588	-0.806	0.067
C(3)	1	0.284	-0.161	0.201	-0.966
	2	0.245	-0.964	-0.241	0.110
	3	0.217	-0.211	0.949	0.233
C(4)	1	0.256	0.545	-0.316	0.778
	2	0.247	0.806	-0.058	-0.589
	3	0.209	0.231	0.947	0.223
C(5)	1	0.268	-0.188	0.346	0.919
	2	0.236	-0.109	0.923	-0.370
	3	0.229	-0.976	-0.169	-0.136
C(6)	1	0.263	-0.006	-0.079	-0.997
	2	0.221	-0.653	-0.755	0.063
	3	0.209	-0.758	0.651	-0.047
N	1	0.237	0.217	-0.158	-0.963
	2	0.224	0.976	0.050	0.211
	3	0.189	0.015	-0.986	0.165
Cl	1	0.225	-0.600	0.656	0.458
	2	0.216	-0.269	0.373	-0.888
	3	0.212	-0.753	-0.656	-0.048

The scattering factors for Cl<sup>-</sup>, N and C were taken from *International Tables for X-ray Crystallography* (1962), and those for H from Stewart, Davidson & Simpson (1965).

### Discussion

The bond lengths, bond angles (and their standard errors) and the torsion angles involving the nonhydrogen atoms are given in Table 6. For comparison, the bond lengths and angles obtained by Shimada *et al.* (1955) are also tabulated. The bond lengths and angles involving the hydrogen atoms are listed in Table 7. The average errors in these are:  $\sigma(C-H) = \sigma(N-H) = 0.07 \text{ \AA}$ ,  $\sigma(C-C-H) = \sigma(N-C-H) = 2.8^\circ$ ,  $\sigma(H-C-H) = 3.5^\circ$ . A rigid body analysis of the thermal motion (Schomaker & Trueblood, 1968) has been made and the T and  $\omega$  tensors are listed in Table 8. It is found that the translation is nearly isotropic whereas there is a libration of  $6.5^\circ$  about an axis roughly along the line joining C(1)-C(4). This is a reasonable mode of libration in view

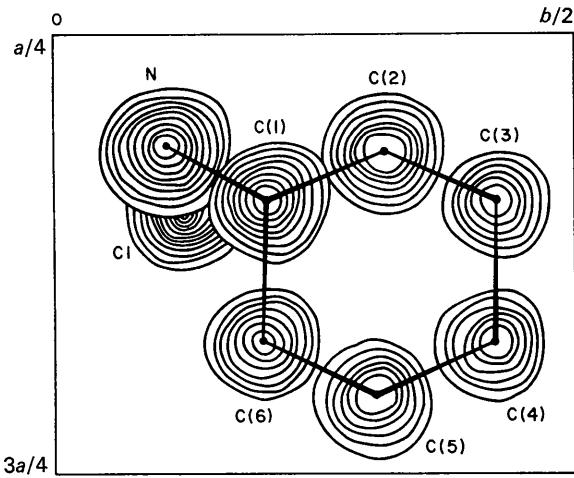


Fig. 3. A perspective view of the electron density as viewed along the  $c$  axis. The contours around Cl<sup>-</sup> start at  $5 \text{ e.} \text{\AA}^{-3}$  and are at intervals of  $2 \text{ e.} \text{\AA}^{-3}$ ; those around other atoms start at  $1 \text{ e.} \text{\AA}^{-3}$  and are at intervals of  $1 \text{ e.} \text{\AA}^{-3}$ .

Table 5. Observed and calculated structure factors  
Each line gives the running index  $k$ ,  $10|F_0|$  and  $10|F_c|$ .

	$0 \times k + 0$	$1 \times 89$	$69$	$4 \times K + 1$	$5 \times 362$	$357$	$7 \times K + 2$	$8 \times 295$	$322$	$9 \times 133$	$118$	$4 \times 60$	$67$	$9 \times K + 5$	$1 \times K + 7$						
1	396	417	8	118	103	0	200	205	7	555	506	1	401	393	1	176	166				
2	845	925	5	202	208	1	721	720	8	168	163	2	367	365	2	243	240				
3	575	657	6	99	99	8	100	99	9	156	156	3	252	250	3	235	235				
4	1368	1825	9	127	137	3	595	553	10	142	131	4	366	353	2	143	151				
5	628	560	10	67	56	4	651	645	11	399	395	5	145	138	5	267	262				
6	7	699	641	6	60	533	336	237	222	6	140	148	1	294	304	1	236	240			
7	6	60	623	7	301	326	15	178	170	1	158	158	0	317	309	2	119	140			
8	9	706	633	7	301	326	15	178	170	1	158	158	0	304	448	8	89	81			
9	10	327	302	1	289	275	8	419	447	1	K + 2	9	75	67	1	250	246				
11	11	472	423	2	380	373	9	89	71	1	718	740	6	115	118	3	223	206			
12	12	242	252	3	243	238	10	144	153	2	412	401	8	92	95	4	250	246			
13	13	208	193	4	52	51	11	137	137	3	240	242	10	84	93	5	185	134			
14	5	5	103	91	12	146	154	1	148	148	2	244	276	8	178	162					
15	6	6	63	59	12	146	154	4	602	595	1	155	142	10	9	110	98				
16	1	1	129	141	5	245	271	2	59	55	4	167	169	10	9	196	191				
17	2	253	273	1	125	125	6	125	125	5	245	271	11	178	179	5	152				
18	2	854	807	9	126	128	1	635	625	7	98	98	4	168	183	7	100	94			
19	3	617	641	10	163	162	2	171	169	8	96	88	5	118	122	8	79	83			
20	4	292	281	3	203	209	9	174	177	7	98	99	1	343	325	3	121	117			
21	5	555	555	8	202	205	10	154	140	8	102	102	10	356	355	2	167	166			
22	6	500	507	9	174	174	5	91	95	8	96	96	9	320	319	3	121	120			
23	7	263	254	0	147	163	6	98	94	13	79	56	0	384	399	3	171	166			
24	8	156	166	1	112	102	8	76	99	1	183	186	4	126	135	6	155	152			
25	9	149	149	3	209	209	9	122	121	2	148	148	7	178	182	8	75	67			
26	10	144	144	5	96	96	10	152	162	2	148	148	9	321	321	5	105	106			
27	11	58	61	5	58	58	0	128	145	3	78	80	9	96	95	2	103	95			
28	2	7	101	116	6	146	146	1	486	483	4	55	41	10	83	91	0	79	68		
29	3	6	100	101	2	156	156	5	124	122	10	155	166	9	197	207	1	212	207		
30	4	0	376	388	2	156	156	9	104	104	0	463	478	1	K + 6	4	100	94			
31	5	1	585	572	4	505	507	2	156	156	0	336	334	3	132	131	3	79	83		
32	6	1	393	191	5	182	191	10	139	133	2	152	156	2	51	51	3	120	116		
33	7	3	1142	1200	1	156	152	5	574	577	6	113	119	3	152	156	3	284	283		
34	8	4	55	55	2	188	188	7	154	154	0	201	195	4	141	147	4	205	211		
35	9	5	178	174	3	110	103	6	231	208	8	236	231	1	391	371	2	145	143		
36	10	6	73	66	4	50	50	20	275	281	9	217	228	3	122	120	7	160	159		
37	7	7	351	355	11	114	114	11	408	408	12	225	220	10	100	100	4	274	258		
38	8	7	257	257	12	171	169	12	171	169	17	174	174	5	311	311	8	201	197		
39	9	7	49	49	17	10	92	107	9	107	107	9	117	117	6	169	178	10	83	78	
40	10	62	54	11	130	134	3	K + 2	9	110	117	7	132	129	0	485	500	5	105	95	
41	11	239	236	10	K + 0	0	128	128	1	179	179	8	147	147	9	98	102	4	K + 7	4	
42	12	176	173	7	K + 1	1	663	616	2	151	151	5	240	240	2	283	289	2	113	106	
43	13	195	189	195	3	125	126	11	126	113	3	411	396	0	395	390	3	106	105		
44	14	3	144	144	2	175	171	2	297	277	5	721	691	5	155	156	3	121	120		
45	15	4	155	164	164	164	164	157	335	335	1	303	303	1	243	238	4	129	136		
46	1	1063	1115	5	98	100	4	213	216	6	446	473	9	324	315	1	202	202			
47	2	845	837	5	100	104	5	163	163	7	206	200	6	165	168	2	159	157			
48	3	640	636	1	265	274	8	93	97	9	509	488	6	152	157	3	131	142			
49	4	268	259	5	163	163	5	163	163	8	246	246	8	181	181	4	141	145			
50	5	5	133	93	99	9	103	103	10	121	121	10	121	121	5	251	263	5	109	108	
51	6	59	59	1	103	98	52	24	217	18	156	156	13	151	157	6	204	204	6	104	103
52	7	599	519	2	1510	1514	9	96	96	93	11	109	105	12	138	138	7	102	107		
53	8	729	244	3	346	358	10	54	72	12	75	60	11	6	251	263	8	109	108		
54	9	79	68	4	476	476	11	12	12	75	67	6	175	178	9	149	148	5	K + 8	4	
55	10	12	12	4	K + 1	5	311	305	5	249	245	7	225	219	1	284	284	1	225	216	
56	11	12	12	4	K + 2	6	277	277	8	156	156	6	439	433	1	281	277	1	225	216	
57	12	12	12	4	K + 3	7	163	163	9	166	166	7	225	225	2	297	301	3	59	57	
58	13	12	12	4	K + 4	8	170	168	10	166	166	9	167	167	3	213	219	4	66	66	
59	14	12	12	4	K + 5	9	177	177	10	228	235	10	126	130	1	317	317	4	137	137	
60	15	12	12	4	K + 6	10	275	289	11	165	161	10	40	40	8	76	63	2	255	262	
61	16	12	12	4	K + 7	11	275	289	12	165	161	11	40	40	9	65	66	4	125	135	
62	17	12	12	4	K + 8	12	275	289	13	165	161	12	40	40	10	63	62	5	116	117	
63	18	12	12	4	K + 9	13	275	289	14	165	161	13	40	40	11	62	61	6	116	116	
64	19	12	12	4	K + 10	14	275	289	15	165	161	14	40	40	12	61	60	7	116	116	
65	20	12	12	4	K + 11	15	275	289	16	165	161	15	40	40	13	60	59	8	116	116	
66	21	12	12	4	K + 12	16	275	289	17	165	161	16	40	40	14	59	58	9	116	116	
67	22	12	12	4	K + 13	17	275	289	18	165	161	17	40	40	15	58	57	10	116	116	
68	23	12	12	4	K + 14	18	275	289	19	165	161	18	40	40	16	57	56	11	116	116	
69	24	12	12	4	K + 15	19	275	289	20	165	161	19	40	40	17	56	55	12	116	116	
70	25	12	12	4	K + 16	20	275	289	21	165	161	20	40	40	18	55	54	13	116	116	
71	26	12	12	4	K + 17	21	2														

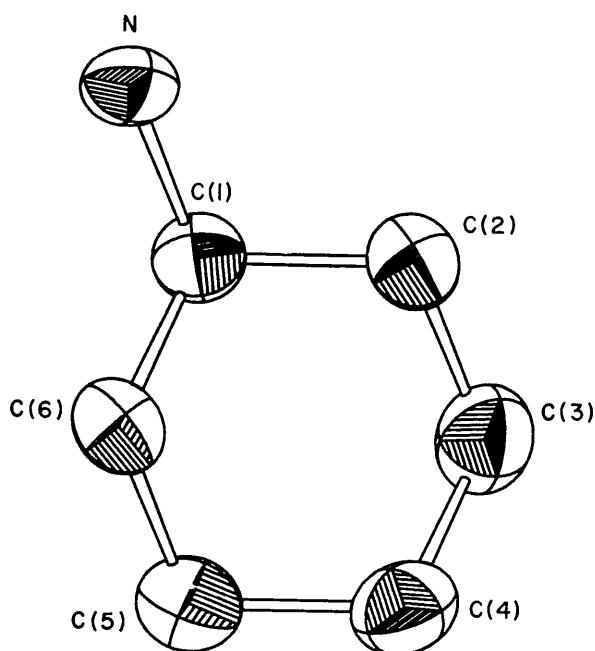


Fig. 4. ORTEP plot of the molecule.

of the hydrogen-bonding scheme involving the amino group. The values corrected for librational motion are given in parentheses in Table 6. It is found that the C(4)-C(5) bond is still short, differing from the remaining ring bonds by about  $2.5\sigma$ , although chemically the C(4)-C(5) bond is similar to the C(3)-C(4) bond. The average corrected values of the endocyclic bond distance, bond angle, and torsional angle are  $1.523 \pm 0.007 \text{ \AA}$ ,  $111.3 \pm 0.6^\circ$  and  $55.0 \pm 1.2^\circ$ , respectively. The average bond distance and bond angle obtained in the

projection work are  $1.55 \text{ \AA}$  and  $110^\circ$  respectively (Shimada *et al.*, 1955). Although the present results are more accurate, the differences between our values and those of Shimada *et al.* (1955) are probably within the

Table 7. Bond lengths and angles involving the hydrogen atoms

	Distance	Angle
C(1)-H(1)	$0.89 \text{ \AA}$	H(1)-C(1)-N
C(2)-H(2)	$0.98$	H(1)-C(1)-C(2)
C(2)-H(2')	$1.02$	H(1)-C(1)-C(6)
C(3)-H(3)	$0.87$	H(2)-C(2)-C(1)
C(3)-H(3')	$1.13$	H(2)-C(2)-C(3)
C(4)-H(4)	$1.12$	H(2)-C(2)-H(2')
C(4)-H(4')	$0.95$	H(2')-C(2)-C(1)
C(5)-H(5)	$0.85$	H(2')-C(2)-C(3)
C(5)-H(5')	$1.05$	H(3)-C(3)-C(2)
C(6)-H(6)	$1.03$	H(3)-C(3)-C(4)
C(6)-H(6')	$0.90$	H(3)-C(3)-H(3')
N-HN(1)	$1.10$	H(3)-C(3)-C(2)
N-HN(2)	$1.02$	H(3')-C(3)-C(4)
N-HN(3)	$0.94$	H(4)-C(4)-C(3)
		H(4)-C(4)-C(5)
		H(4)-C(4)-H(4')
		H(4')-C(4)-C(3)
		H(4')-C(4)-C(5)
		H(5)-C(5)-C(4)
		H(5)-C(5)-C(6)
		H(5)-C(5)-H(5')
		H(5')-C(5)-C(4)
		H(5')-C(5)-C(6)
		H(6)-C(6)-C(5)
		H(6)-C(6)-C(1)
		H(6)-C(6)-H(6')
		H(6')-C(6)-C(5)
		H(6')-C(6)-C(1)
		HN(1)-N-C(1)
		HN(1)-N-HN(2)
		HN(1)-N-HN(3)
		HN(2)-N-C(1)
		HN(2)-N-HN(3)
		HN(3)-N-C(1)

Table 6. Bond lengths, bond angles and torsion angles involving the nonhydrogen atoms

Values in parentheses are those corrected for librational motion of the molecule.

	Bond length			Bond angle			Shimada <i>et al.</i> (1955) ( $\pm 5^\circ$ )
	This work	$\sigma(l)$	Shimada <i>et al.</i> (1955) ( $\pm 0.05 \text{ \AA}$ )	This work	$\sigma(\theta)$		
C(1)-C(2)	$1.516 \text{ \AA}$ ( $1.526$ )	$0.008 \text{ \AA}$	$1.55 \text{ \AA}$	C(1)-C(2)-C(3)	$110.8^\circ$ ( $110.7$ )	$0.5^\circ$	$113^\circ$
C(2)-C(3)	$1.521$ ( $1.526$ )	$0.010$	$1.55$	C(2)-C(3)-C(4)	$111.3$ ( $111.1$ )	$0.5$	$108$
C(3)-C(4)	$1.520$ ( $1.529$ )	$0.009$	$1.54$	C(3)-C(4)-C(5)	$112.2$ ( $112.4$ )	$0.5$	$109$
C(4)-C(5)	$1.493$ ( $1.502$ )	$0.009$	$1.55$	C(4)-C(5)-C(6)	$112.4$ ( $112.2$ )	$0.5$	$110^*$
C(5)-C(6)	$1.523$ ( $1.528$ )	$0.010$	$1.55^*$	C(5)-C(6)-C(1)	$110.4$ ( $110.2$ )	$0.5$	$111^*$
C(6)-C(1)	$1.518$ ( $1.527$ )	$0.006$	$1.54$	C(6)-C(1)-C(2)	$111.1$ ( $111.3$ )	$0.5$	$106^*$
C(1)-N	$1.488$ ( $1.493$ )	$0.008$	$1.45$	C(2)-C(1)-N	$110.0$ ( $109.9$ )	$0.5$	$102^*$
				C(6)-C(1)-N	$109.9$ ( $109.7$ )	$0.5$	$109$

Atoms	Torsion angle
C(5)-C(6)-C(1)-C(2)	$56.3^\circ$ ( $56.5$ )
C(6)-C(1)-C(2)-C(3)	$-57.0$ ( $-57.2$ )
C(1)-C(2)-C(3)-C(4)	$54.8$ ( $54.8$ )
C(4)-C(5)-C(6)-C(1)	$-54.7$ ( $-54.7$ )
C(2)-C(3)-C(4)-C(5)	$-53.3$ ( $-53.5$ )
C(3)-C(4)-C(5)-C(6)	$53.5$ ( $53.7$ )
N-C(1)-C(2)-C(3)	$-179.0$ ( $-179.0$ )
N-C(1)-C(6)-C(5)	$178.4$ ( $178.4$ )

\* Values not in agreement with those published.

probable errors of the earlier work. Davis & Hassel (1963) have found, from electron diffraction studies on cyclohexane systems, values which are very similar to those obtained in the present investigation. It is noteworthy that the valency angle is significantly larger than the ideal tetrahedral value of  $109^{\circ}28'$ .

The cyclohexane ring is in the chair form with the amino group equatorially substituted. The average value of the torsional angle in this compound agrees well with the value of  $55.2^{\circ}$  expected for a regular cyclohexane ring with C-C-C valence angles of  $111.3^{\circ}$ . Table 6 shows that the torsional angles around the bonds C(6)-C(1) and C(1)-C(2) involving the substituted atom are approximately equal and are about  $3^{\circ}$  greater than those at the opposite end, involving C(4). The departure of the individual torsional angles from the mean value is such that there is a greater puckering involving the equatorially substituted atom,

while a reduction in puckering occurs at the opposite end.

Drawings showing the crystal packing have already been given in the earlier paper by Shimada *et al.* (1955). The ammonium group has three neighboring chloride ions at characteristic distances of 3.21, 3.14 and 3.20 Å, Table 9. A view of the surroundings of the ammonium group as viewed down the C(1)-N bond is given in Fig. 5. The hydrogen bonds are not all linear, the angles at the hydrogen atoms being 169, 179 and 168°. Each  $\text{NH}_3^+$  group is surrounded by three  $\text{Cl}^-$  ions forming a distorted triangular pyramid and *vice versa*. The structure is quite loosely packed as is evident from the low density, and there are no unusually short intermolecular contacts. An interesting comparison of the crystal structures of the higher- and lower-membered alkylamine hydrohalides with those of the alkali halides has been presented by Shimada *et al.* (1955).

Table 8.  $\tau$  and  $\omega$  tensors and their eigenvalues and eigenvectors

Standard deviations are given in parentheses.

$T = (\text{\AA})^2$	$\begin{bmatrix} 0.046 \\ (0.002) & 0.002 \\ & (0.001) & 0.004 \\ & 0.043 & (0.001) \\ & & 0.001 \\ & & 0.047 \\ & & (0.003) \end{bmatrix}$
$\omega = (\text{deg})^2$	$\begin{bmatrix} 19.9 \\ (3.8) & 17.0 \\ & (2.4) & 5.6 \\ & 34.2 & (2.6) \\ & (6.2) & 4.2 \\ & & (3.4) \\ & & 9.6 \\ & & (2.7) \end{bmatrix}$

Principal values and components of eigenvectors

$\text{\AA}^2$	$\text{\AA}$	$T$	$l$	$m$	$n$	$(\text{deg})^2$	$(\text{deg})$	$l$	$\omega$	$m$	$n$
0.051	0.23	-0.657	-0.187	-0.730		46.7	6.8	0.554	0.814	0.176	
0.043	0.21	-0.341	-0.790	0.509		10.8	3.3	0.523	-0.504	0.617	
0.042	0.20	-0.672	0.584	0.455		6.2	2.5	0.647	-0.289	-0.705	

Table 9. Hydrogen bond distances and angles

The first atom is in the list given in Table 3 and the second atom is symmetry-related according to the following code:

Atom	Code	Distance	Atom	Angle
N—Cl	I	3.21 Å	C(1)—N—Cl	$100.6^{\circ}$
H(1)—Cl	I	2.12	H(1)—N—Cl	7.2
			N—H(1)—Cl	169.1
N—Cl	II	3.14	C(1)—N—Cl	109.9
H(2)—Cl	II	2.12	H(2)—N—Cl	0.5
			N—H(2)—Cl	179.2
N—Cl	III	3.20	C(1)—N—Cl	110.9
H(3)—Cl	III	2.27	H(3)—N—Cl	8.8
			N—H(3)—Cl	167.5

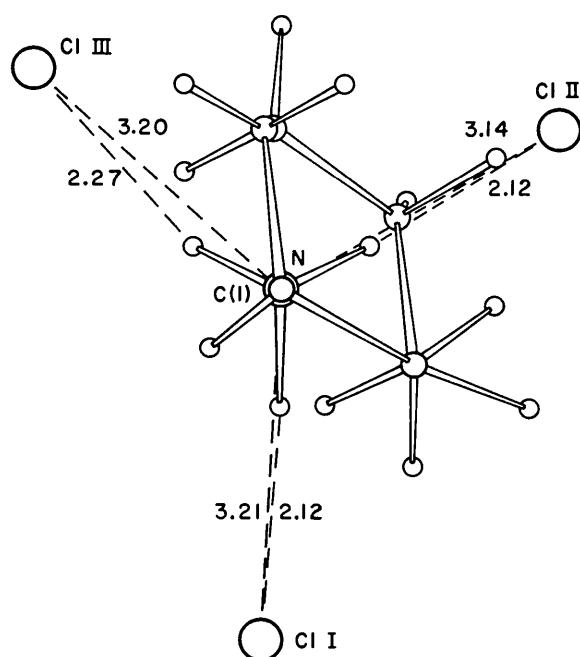


Fig. 5. The surroundings of the  $\text{NH}_3^+$  group as viewed along the bond  $\text{N}-\text{C}(1)$ .

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## Modifications and Transitions of Solid Oxygen

BY ERWIN M. HÖRL

*Österreichische Studiengesellschaft für Atomenergie, Institut Metallurgie, Reaktorzentrum Seibersdorf, Austria*

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Thin films of solid oxygen were investigated by electron diffraction and electron microscopy. New information was obtained about the formation of the modifications of solid oxygen and the transitions between the modifications. In particular, the phase which is formed on helium-cooled substrates by deposition of oxygen gas at a low flow rate was examined.

### Introduction

The author has shown in previous papers (Hörl, 1959, 1962; Hörl & Marton, 1961) how electron diffraction can be applied to problems of crystal structure, crystal growth and crystal faults of solidified permanent gases. The present paper presents a further study of the modifications of solid oxygen with the aim of investigating the transitions between these modifications in thin films.

The technique described in the previous papers (see also Hörl & Marton, 1958) was extended by the use of an electron microscope as diffraction apparatus. A special stage (Hörl, 1968) for cooling specimens with liquid helium was constructed, which also allowed magnetic studies (not discussed in this paper) by the application of a transverse magnetic field. With this stage it

was possible to obtain, in addition to the electron diffraction patterns, electron micrographs of the deposits of interest. Direct observation of the crystals also allowed selected area diffraction.

### Oxygen modifications

Ten years ago there were three known modifications of solid oxygen: an  $\alpha$  modification, stable up to  $23.9^\circ\text{K}$ , a  $\beta$  modification stable between  $23.9^\circ$  and  $43.6^\circ\text{K}$  and a  $\gamma$  modification stable between  $43.6^\circ\text{K}$  and the melting point at  $54.4^\circ\text{K}$ . Today we have to add two additional modifications, one (we will call it  $\alpha'$ ) which is formed in the temperature range of the  $\alpha$  phase when oxygen gas is deposited in the form of a very thin film on a cold substrate, and an amorphous phase, which can be ob-